

The Economic Effects of Firm-Level Uncertainty: Evidence Using Subjective Expectations

Giuseppe Fiori* Filippo Scocianti

May 6, 2023

Abstract

Using over two decades of Italian survey data on business managers' expectations we measure *subjective* firm-level uncertainty and quantify its economic effects. Firm-level uncertainty persists for a few years and varies across firms' demographic characteristics. Uncertainty induces sizable and long-lasting economic effects over a broad array of real and financial variables only when driven by its *downside* component—that is, uncertainty about future adverse outcomes. Economy-wide uncertainty, constructed aggregating firm-level uncertainty, is countercyclical but uncorrelated with typical proxies in the literature.

JEL Classification: D24; E22; E24.

Keywords: Uncertainty, business cycles, investment, expectations, cash holdings, downside uncertainty.

*Corresponding author: Giuseppe Fiori, Board of Governors of the Federal Reserve System, Division of International Finance, 20th and C Sts. NW, Washington DC 20551, United States (email: giuseppe.fiori@frb.gov; webpage: <http://www.giuseppefiori.net>). Filippo Scocianti: Banca d'Italia, Via Nazionale 91, Rome, Italy. First version: April 13, 2020. We are grateful to the Associate Editor Cosmin Ilut, an anonymous referee, our formal discussants Steve Davis and Steffen Henzel, Danilo Cascaldi-Garcia, Brian Doyle, Thiago Ferreira, Matteo Iacoviello, Cosmin Ilut, Nir Jaimovich, Andrea Lanteri, Francesca Lotti, Shannon Luk, Hyunseung Oh, Andrea Prestipino, Plutarchos Sakellaris, Enrico Sette, Frank Warnock, and participants to various seminars and conferences for useful comments. The views expressed in this paper are solely the responsibility of the authors and should not be interpreted as reflecting the views of the Board of Governors of the Federal Reserve System (or of any other person associated with the Federal Reserve System) or the Bank of Italy.

1 Introduction

Economic theory emphasizes that uncertainty about future macroeconomic and microeconomic outcomes shapes firms' decisions. Economic uncertainty has a long tradition in economics, and, on the heels of [Bloom \(2009\)](#), a vast literature has improved the measurement and understanding the nature of and economic consequences of macroeconomic, or aggregate, time-varying uncertainty. The literature on *firm-level* uncertainty is scant and limited mainly by data availability.

We advance the literature on subjective uncertainty by using Italian survey data on firm-level expectations that span over 20 years and cover multiple business cycle episodes to study the properties and economic effects of firm-level uncertainty.¹ The granularity of our data allows us to tease out the effects of uncertainty from a plethora of confounding factors, including past business conditions, changes in the first moment of the probability distribution of future sales, and firm-specific characteristics. Our analysis yields three main insights on the persistence of firm-level uncertainty, its economic effects, and the properties of aggregate uncertainty across business cycles.

First, we construct a measure of ex ante firm-level uncertainty using survey data on managers' expectations about future sales for a representative sample of Italian firms. Firm-level uncertainty is a persistent process that lasts for a few years. The level of firms' uncertainty about their future business prospects depends upon demographic characteristics, such as age, size, and the sector in which firms operate.

Second, the detrimental effects of higher firm-level uncertainty over a broad set of real

¹The Bank of Italy survey constitutes a unicum in the existing literature, as most surveys that track uncertainty on firm-level outcomes span only a few years. In particular, for the United States, [Altig et al. \(2022\)](#) developed a monthly panel Survey of Business Uncertainty (SBU) starting in 2014 that features about 1,750 firms in 50 states. In Germany, the IFO Institute surveyed firms' expectations from 2013 to 2016, see [Bachmann et al. \(2018\)](#) and [Bachmann et al. \(2020\)](#). A longer monthly time-series starting in 1980 and based on qualitative expectations is used in [Bachmann et al. \(2013\)](#) and [Massenot and Pettinicchi \(2018\)](#). The Decision Maker Panel (DMP) survey was launched for the United Kingdom in August 2016.

22 and financial outcomes occur when the increase in total uncertainty is driven by its down-
23 side component—the part of the uncertainty accounted for by below mean outcomes. The
24 firm is instead insensitive to changes in upside uncertainty. In this sense, *not all uncertain-*
25 *ties are alike*. An increase in (downside) uncertainty predicts a contemporaneous reduction in
26 total hours (both in the number of workers and hours per worker), a decrease in capacity uti-
27 lization, and cash hoarding for a few periods. With a lag, firms reduce capital accumulation
28 for a few years.

29 Third, we construct an *economy-wide* measure of uncertainty for the Italian economy,
30 aggregating individual firm-level data, and find it to be countercyclical. While this coun-
31 tercyclicality reproduces the literature’s typical result, we emphasize that our bottom-up
32 aggregate uncertainty is uncorrelated to measures of cross-sectional dispersion, which are
33 standard proxies for macroeconomic uncertainty employed in the literature. This lack of
34 correlation suggests that much of the variation in cross-sectional measures is not driven by
35 ex ante uncertainty.

36 The source of the data on expectations is the Survey of Industrial and Service Firms (or
37 INVIND), an extensive annual business survey conducted by the Bank of Italy on a sam-
38 ple of Italian firms representative of the aggregate economy. As discussed in Section 2, the
39 survey elicits managers’ expectations over the average, the minimum, and the maximum
40 one-year-ahead sales growth rates. Thus, we directly observe the first moment of the subjec-
41 tive probability distribution of future sales and the range between the maximum and min-
42 imum or max–min range, around the mean prediction. Expectations are informative about
43 the mean and the uncertainty in firm-level outcomes as there is no systematic bias in firms’
44 expectations, and realized ex post sales fall in the ex ante max–min range in about 75 percent
45 of observations. Using the 2005 and 2017 waves of INVIND that elicited the *full* probability
46 distribution of expected sales, we show that the max–min range measures the dispersion of

47 future expected outcomes while being orthogonal to the third moment of the distribution,
48 or skewness. An equivalent strategy shows that the gap between the average and the min-
49 imum, and the maximum and the average of expected sales are the main determinants of
50 the downside and upside component of uncertainty, respectively. The nearly deterministic
51 relationship between the max–min range and the dispersion of future sales and between the
52 proxies of the downside and upside uncertainty allows us to use the max–min range and its
53 components to measure firm-level uncertainty for the whole sample. Directly observing the
54 first and the second moments of the distribution of expected outcomes enable us to over-
55 come one of the existing literature’s main challenges, disentangling the economic effect of
56 fluctuations in uncertainty from changes to the first moment. Also, the panel structure of
57 our data allows us to control for firm-specific and sectoral effects as well as time effects.

58 Our first insight is to show that uncertainty and its components are persistent processes
59 by fitting an autoregressive process of order one and exploiting the 2017 wave of INVIND.
60 The 2017 wave elicits the full probability distribution of expected sales one year ahead and
61 three years ahead, allowing us to study how uncertainty about 2020 sales evolved from 2017
62 to 2019. We view both approaches as complimentary as they offer different strengths re-
63 lated to the sample length and bias in the estimated yearly persistence with panel data. We
64 balance these considerations and take 0.56, an average of the estimates obtained with each
65 approach, as our best estimate for the persistence of overall firm-level uncertainty. Similar
66 results apply to downside and upside uncertainty, implying a half-life of a shock to uncer-
67 tainty equal to about one year and a half.

68 Our second insight indicates that firm-level uncertainty has sizable and persistent eco-
69 nomic effects across a broad array of real and financial variables. Matching INVIND with
70 balanced sheets data allows us to perform panel regression analysis at various horizons and
71 broaden the scope of the analysis to real and financial outcomes. Our findings indicate that a

72 one standard deviation increase in uncertainty predicts a drop in utilization and total hours
73 of about 1 percent and, with a lag, a drop in investment of about 3 percent in each of the
74 following two years. Cash holdings increase on impact and then return to initial levels after
75 two years. Our closest antecedent is [Alfaro et al. \(2017\)](#), who studies the effect of firm-level
76 uncertainty on real and financial outcomes to one year out horizon. Relative to [Alfaro et al.](#)
77 [\(2017\)](#), our estimate results on the effects of uncertainty on investment to be twice as large
78 one year out and even more detrimental on real variables considering the full horizon of our
79 estimates. Concerning cash holdings, we find smaller effects of uncertainty.

80 The differentiated response and the persistence of the estimated effects of the downside
81 uncertainty provide practical overidentifying restrictions against which to test competing
82 models to quantify uncertainty's effects. Two points are worth highlighting. First, the im-
83 mediate fall in hours following an increase in uncertainty indicates that labor is not deter-
84 mined purely by static variables; rather, it behaves like a durable input similar to capital.
85 Second, our evidence on the sensitivity of firms to downside uncertainty emphasizes costly
86 downsizing of capital or labor, such as the one induced by input irreversibility and the en-
87 suing "bad news principle" discussed by [Bernanke \(1983\)](#). Other mechanisms are consistent
88 with our results. Downside uncertainty may also increase the likelihood of firms becoming
89 financially constrained in the future, leading to a decrease in the accumulation of inputs;
90 see, for instance, [Alfaro et al. \(2017\)](#) and [Christiano et al. \(2014\)](#). Also, to the extent that the
91 minimum of future sales is interpreted as a summary statistic of the worst-case scenario, the
92 sensitivity to downside uncertainty may be loosely interpreted as agreeing with the predic-
93 tions of theories that emphasize ambiguity aversion, as in [Hansen et al. \(1999\)](#) and [Ilut and](#)
94 [Schneider \(2014\)](#). In those models, agents form beliefs over a range of possible scenarios and
95 act as if the worst scenario will occur.

96 Our third insight indicates that much of the variation in the cross-sectional dispersion

97 is not linked to uncertainty. Our bottom-up measure of aggregate uncertainty about fu-
98 ture sales is countercyclical, increasing sharply during economic crises, such as the Great
99 Financial Crisis and the latest COVID-19 recession, as well as periods with elevated political
100 uncertainty. The little correlation between our proxy and measures of cross-sectional disper-
101 sion points to a disconnection between ex ante uncertainty and realized risk at the *aggregate*
102 level. At the firm level, we find a positive but quantitatively small relationship between
103 current uncertainty and the size of future absolute forecast errors, a proxy of realized risk.
104 The small quantitative link rationalizes the little correlation between ex ante uncertainty and
105 cross-sectional dispersion. Our evidence agrees which uncertainty ex ante does not neces-
106 sarily result in realized ex post risk such as [Ilut and Schneider \(2014\)](#) and [Ilut and Saijo \(2021\)](#)
107 based on ambiguity aversion, or the work of [Angeletos et al. \(2018\)](#).

108 The paper is organized as follows. In Section 1.1, we review the existing literature. In
109 Section 2, we describe the data. In Section 3, we detail the construction of our measure of
110 ex ante uncertainty based on subjective expectations. We characterize the economic effects
111 of uncertainty and its components in Sections 4 and 5, respectively. In Section 6, we discuss
112 the implications of our results for macroeconomic modeling. In Section 7, we construct a
113 measure of aggregate uncertainty based on firm-level uncertainty. Section 8 concludes.

114 1.1 Literature Review

115 Our work connects to many strands of the existing literature on uncertainty and aggre-
116 gate fluctuations. While the current literature provides a sizable number of surveys eliciting
117 consumer expectations, less is known about quantitative measures of uncertainty at the firm
118 level.² Our data source INVIND is the forerunner of the DMP for the United Kingdom

²Examples of consumer surveys include the U.S. Health and Retirement Study ([Hurd and McGarry, 2002](#)), the Bank of Italy's Survey on Household Income and Wealth ([Guiso et al., 1992](#); [Guiso et al., 2002](#)), the Survey of Economic Expectations ([Dominitz and Manski, 1994](#)), the University of Michigan Surveys of Consumers ([Dominitz and Manski, 2004](#)) and the New York Fed's very recent Survey of Consumer Expectations ([Armantier et al., 2015](#)).

119 discussed in [Altig et al. \(2020\)](#) and SBU for the United States described in [Altig et al. \(2022\)](#).
120 Another important example is the IFO survey employed in [Bachmann et al. \(2018\)](#) and [Bach-](#)
121 [mann et al. \(2020\)](#). [Holzmeister et al. \(2020\)](#) uses survey data to study how risk is perceived
122 by financial professionals emphasizing that skewness of expected returns determines their
123 perception of risk.³ The critical advantage of INVIND is that it has surveyed firms' expecta-
124 tions for over two decades, allowing us to study how uncertainty has evolved over multiple
125 business cycles. In contrast, DMP and SBU started only recently, albeit at a higher frequency.

126 In using survey data to study the economic outcomes of subjective uncertainty, our pa-
127 per builds on the pioneering work of [Guiso and Parigi \(1999\)](#) and [Bontempi et al. \(2010\)](#).⁴
128 Relative to these contributions that also use INVIND, the panel dimension of our sample
129 allows us to expand the scope of the analysis characterizing the effect of uncertainty on a
130 broad array of real and financial variables beyond investment. Besides, we show that the
131 source of uncertainty matters for its economic effects, with only the downside component of
132 uncertainty having sizable economic effects.

133 A second strand of the literature has investigated the economic effects of uncertainty,
134 typically focusing on investment and pointing to a negative uncertainty-investment rela-
135 tionship when dealing with micro-level uncertainty. Studies differ on the measure of firm-
136 level uncertainty with [Leahy and Whited \(1996\)](#) and [Bloom et al. \(2007\)](#) using realized stock
137 return volatility; [Stein and Stone \(2013\)](#) using the option price; and [Gulen and Ion \(2016\)](#)
138 using the policy uncertainty index developed by [Baker et al. \(2016\)](#).

139 Moreover, firm-level uncertainty appears to vary in both the cross section and the time
140 series. [Bachmann et al. \(2017\)](#) and [Senga \(2015\)](#) find substantial cross-sectional heterogeneity
141 and time variation in measures of firm-idiosyncratic uncertainty using survey data. [Senga](#)

³[Ben-David and Graham \(2013\)](#) and [Gennaioli et al. \(2016\)](#) study executives' stock return expectations.

⁴Another example is [Morikawa \(2013\)](#) who uses two-point distributions from the survey conducted at the Research Institute of Economy, Trade and Industry. He focuses on uncertainty related to the tax system and trade policy matters for firms' capital investments and overseas activities.

142 (2015) also finds that smaller and younger firms face greater uncertainty.

143 Besides differences in the considered measure of uncertainty, our analysis shows that the
144 effects of uncertainty extend beyond capital accumulation and affect the labor market and
145 financial decisions. The broad focus on firm-level economic outcomes aligns our work with
146 [Alfaro et al. \(2017\)](#) with three critical distinctions related to our uncertainty measure. First,
147 rather than relying on the *realized* or implied annual volatility of stock returns, we employ
148 an ex ante measure of uncertainty that allows us to tease out changes in the dispersion of
149 expected outcomes from fluctuations in the first moment of future expectations. Second,
150 our empirical analysis shows that the economic effects of uncertainty last for a few years,
151 with investment overshooting its steady-state level when the shock is reabsorbed. Third,
152 we distinguish the source of fluctuations in uncertainty between a downside and an upside
153 component, showing that only the former matters for its economic effects.

154 Our work also connects to the literature on aggregate uncertainty and its cyclical prop-
155 erties along the business cycle. A robust finding since, at least, [Bloom \(2009\)](#) is that cross-
156 sectional measures of uncertainty rise in recessions. [Bloom et al. \(2018\)](#) find countercyclical
157 establishment-level total factor productivity shocks is countercyclical (see also [Kehrig \(2015\)](#)
158 and [Bloom \(2014\)](#)). [Bachmann et al. \(2013\)](#) proxy for aggregate uncertainty with forecaster
159 disagreement and find that the latter is higher in downturns. [Hassan et al. \(2019\)](#) and [Baker
160 et al. \(2016\)](#) develop a measure of uncertainty using textual analysis focusing on political
161 risk and economic policy uncertainty.⁵ We refer the reader to a comprehensive review of the
162 literature to [Datta et al. \(2017\)](#) and [Fernández-Villaverde and Guerrón-Quintana \(2020\)](#).

⁵In a similar vein of research, [Caldara et al. \(2020\)](#) use textual analysis to explore the quantitative implications of trade policy uncertainty. [Handley and Limão \(2017\)](#) quantify the effects of trade policy uncertainty for the U.S. and Chinese economies using a general equilibrium model.

163 **2 Data: Subjective Firm-Level Expectations**

164 This section describes the data sources that constitute the basis for measuring firm-level
165 uncertainty and quantifying its economic effects. We first provide details about our data
166 source in Section 2.1. Then, we describe the measures of firm-level expectations and establish
167 their validity in Section 2.2 and in Section 2.3, respectively.

168 **2.1 Data Sources**

169 We obtained our data set by combining different sources. We first construct our measure
170 of uncertainty using data on firm-level expectations from INVIND. INVIND is an annual
171 business survey conducted between February and April of every year by the Bank of Italy
172 on a representative sample of firms operating in industrial sectors (manufacturing, energy,
173 and extractive industries), construction, and nonfinancial private services, with the admin-
174 istrative headquarters in Italy. The sample is representative of the Italian economy, based on
175 the branch of activity (according to an 11-sector classification), size class, and region in which
176 the firm's head office is located. We then use detailed information on yearly balance sheets
177 from Cerved Group S.P.A. (Cerved Database) to obtain data on investment (equipment and
178 structures), cash holdings, and realized sales. Total hours, number of employees, and capac-
179 ity utilization are part of INVIND. Industry-specific price deflators are obtained from the
180 Italian National Institute of Statistics. The sample period extends over 20 years, from 1996 to
181 2019. The matched data set includes about 25,000 firm-year observations from an average of
182 more than 900 firms per year. We note that the number of firm-year observations in INVIND
183 depends on the variable of interest and includes more than 35,000 observations. However,
184 not all of the observations can be matched with balance sheet data in Cerved, reducing the
185 sample to about 25,000 observations. Next, we report statistics using the available data and
186 accounting for each firm's share in the population of Italian firms. We refer the reader to

187 Appendix A for more details.

188 2.2 Firm-Level Expectations: Variables Description

189 INVIND elicits expectations about future sales from surveyed firms. Specifically, the
190 survey reports three critical variables for our purposes:

- 191 1. The expected, or *average*, growth rate of sales one year ahead, denoted by $s_{avg,f,t}^e$.
- 192 2. The *maximum*, or best-case scenario, future growth rate of sales one year ahead, de-
193 noted by $s_{max,f,t}^e$.
- 194 3. The *minimum*, or worst-case scenario, future growth rate of sales one year ahead, de-
195 noted by $s_{min,f,t}^e$.

196 Shaped by firm-specific, sectoral, and aggregate factors, these variables allow us to directly
197 observe the *first moment* of the probability distribution of the expected growth rate of sales
198 and the *range* of subjective uncertainty around this point. We emphasize that we do not
199 directly observe the probability mass over the support except for the 2005 and 2017 waves.
200 We overcome this limitation in Section 3 by showing that there is a near-deterministic rela-
201 tionship between the range and the standard deviation, or *second moment*, of the probability
202 distribution of expected sales at the firm level. We connect the range with the dispersion in
203 future sales exploiting the 2005 and 2017 waves of the survey that elicit the entire probability
204 distribution, asking firms to provide a quantitative assessment of their business prospects.
205 Using the same data, we also establish that the minimum and the maximum proxy for the
206 part of the variance of expected sales accounted for by outcomes below mean, or down-
207 side uncertainty, and the remaining part accounted for by outcomes above mean, or upside
208 uncertainty. We now describe the statistical properties of $s_{avg,f,t}^e$, $s_{min,f,t}^e$, and $s_{max,f,t}^e$.

209 2.3 Firm-Level Expectations: Statistical Properties

210 Table 1 reports a set of statistics comparing the realized growth rate of sales, the min-
211 imum (worst-case scenario), the maximum (best-case scenario), and the average expected
212 growth rates of sales. Statistics are reported pooling data for the whole sample and taking
213 into account the INVIND sample weight represented by each firm in the entire population
214 of firms. Growth rates are expressed in percent.

215 We start by describing the properties of $s_{avg,f,t}^e$. The median firm expects sales to grow
216 2.6 percentage points, not far from the median of actual sales. To assess whether managers'
217 expectations display a bias relative to realized sales, we perform a two-sided t-test using
218 two-way clustered standard errors by both firm and date to account for common shocks
219 across firms. The test shows that the gap between the expected and realized sales is not
220 statistically different from zero (p-value 0.21), indicating that there is no systematic bias in
221 the firm forecast.

222 Regarding $s_{min,f,t}^e$ and $s_{max,f,t}^e$ the median firm expects the worst-case scenario to result
223 in a decrease of sales of about 2 percentage points and the best-case scenario in an expan-
224 sion of 5. Also, for both variables, the interquartile range ($P_{75} - P_{25}$) is about 10 percentage
225 points. The interval between best- and worst-case scenario is informative about the uncer-
226 tainty faced by each firm as realized sales one year ahead fall within the max–min range in
227 about 75 percent of the observations. Through the lens of this metric, the max–min range
228 can be interpreted, on average, as firms reporting the 10-90 percentile of expected outcomes.
229 Regarding the correlation of $s_{min,f,t}^e$ and $s_{max,f,t}^e$ with GDP, as shown in Table 1, the $s_{avg,f,t}^e$
230 $s_{min,f,t}^e$ and $s_{max,f,t}^e$ are as procyclical as actual sales.

231 The statistical properties of expectations display sizable differences conditioning on firms'
232 size, age, and the sector in which they operate. based on firms' size, small and medium-sized
233 firms (defined as firms employing between 20 and 50 workers) display an expected growth

234 rate in the worst-case scenario of negative 5 percent, lower than negative 1 percent for large
235 firms (with more than 50 employees).⁶ This property shows despite a similar expected av-
236 erage and maximum growth rate, $s_{avg,f,t}^e$ and $s_{max,f,t}^e$.

237 Small and medium-sized firms do not perfectly overlap with the definition of young
238 firms. Young firms (less than five years) tend to expect higher growth both on average
239 and in the best-case scenario than mature and old ones (more than five years) by about 3
240 percentage points. Intuitively, this outcome lines up with firms' life-cycle dynamics that,
241 conditional on survival, grow to reach their optimal size.

242 Finally, firms in the manufacturing sector expect faster growth (4.28 percent) than those
243 in the service sector (2.55 percent). This result reflects the faster growth rate of sales experi-
244 enced by the manufacturing sector that we conjecture is being driven by the higher degree
245 of international openness relative to the service sector. We refer the reader to Table [A.1](#) in
246 Appendix [B](#) for the full set of results.

247 **3 Firm-Level Uncertainty and Subjective Expectations**

248 We now describe how we use INVIND expectations to construct a time-varying measure
249 of individual firms' subjective uncertainty and provide a set of stylized facts on firm-level
250 uncertainty. In Section [3.1](#), we show that there is a near equivalence in the range between
251 the maximum and minimum future expected sales (or the best- and worst-case scenario,
252 $s_{max,f,t}^e - s_{min,f,t}^e$) and the dispersion (or second moment) of future expected sales. Moreover,
253 the minimum and the maximum expected sales proxy the downside and upside components
254 of overall uncertainty. Exploiting these results, we use the max–min range and its compo-
255 nents as measures of firm-level uncertainty and establish a new set of stylized facts on the
256 properties of uncertainty conditioning across age, size, and sector in which the firms oper-
257 ate in Section [3.2](#). Finally, we analyze how firm-specific and aggregate variables covary with

⁶Because of the design of the survey, we do not observe firms with fewer than 20 employees.

258 uncertainty in Section 3.3 and conclude by showing that uncertainty is a persistent process
259 that does not abate quickly in Section 3.4.

260 3.1 The Max–Min Range Measures Dispersion in Future Expected Sales

261 INVIND provides us with the range between the best- and the worst-case scenario about
262 the expected growth rate of sales one period ahead. We now show that this range, denoted
263 by $\sigma_{max-min,f,t}$, measures the second moment of the probability distribution of expected out-
264 comes. In addition, we decompose overall uncertainty into its upside and downside compo-
265 nents and show that $s_{max,f,t}^e$ and $s_{min,f,t}^e$ proxy for upside and downside uncertainty, respec-
266 tively. To obtain these results, we use data from the 2005 and 2017 waves of INVIND. Unlike
267 other years in our sample, these waves elicited the full probability distribution of expected
268 sales over a discretized support of intervals ranging from less than negative 10 percent to
269 more than 10 percent.⁷

270 We compute the mean, standard deviation, and skewness of the subjective probability
271 distribution of expected sales for every firm. Our calculations are carried out applying stan-
272 dard formulas and using, for each bin, the midpoint of the respective interval and its as-
273 sociated probability.⁸ As we observe the probability distribution of future sales, we do not
274 need to impose any distributional assumption. We regress each moment of the subjective
275 distribution on $\sigma_{max-min,f}$, $s_{min,f}^e$ and $s_{max,f}^e$ pooling the 2005 and 2017 waves of INVIND.

276 The first result in Column 1 of Table 2 is the near equivalence between $\sigma_{max-min,f}$ and the

⁷In 2005, the support of the probability distribution of expected sales x was discretized using 11 bins: ≤ -10 percent, $-10 \text{ percent} < x \leq -6$ percent, $-6 \text{ percent} < x \leq -4$ percent, $-4 \text{ percent} < x \leq -2$ percent, $-2 \text{ percent} < x < 0$ percent, 0 , $0 \text{ percent} < x \leq 2$ percent, $2 \text{ percent} < x \leq 4$ percent, $4 \text{ percent} < x \leq 6$ percent, $6 \text{ percent} < x \leq 10$ percent, ≥ 10 percent. In 2017, the grid between -6 percent and $+6$ percent was finer, with intervals of one percentage point rather than two. By the nature of INVIND, the 2005 and 2017 waves asks agents about *one* distribution of expected outcomes. Bachmann et al. (2020) innovates distinguishing between Bayesian and Knightian agents.

⁸For firms that report positive probability mass in the bins ≤ -10 percent and ≥ 10 percent, we need to assume a lower and an upper bound to compute the midpoint of the interval. We choose -20 and 20 as these values represent the 10th and 90th percentiles of the actual sales distribution, see Table 1. Alternatively, we consider -25 and 25 percent, the same percentiles of a pooled distribution of realized sales in the year before, on, and after the survey was elicited.

277 true standard deviation of the probability distribution $St.Dev.f$. The max–min range mea-
 278 sures the second moment of the probability distribution of future sales: firms with higher
 279 dispersion in expected outcomes also display a wider range of $\sigma_{max-min,f}$. The coefficient on
 280 $\sigma_{max-min,f}$ is statistically significant and the R^2 close to one indicates that the range accounts
 281 for almost the total variance of the dependent variable. Column 2 rules out that the range
 282 captures the skewness, as $\sigma_{max-min,f}$ is virtually orthogonal to the third moment.

283 The second result is that $s_{f,min}^e$ and $s_{f,max}^e$ proxy for overall uncertainty and its compo-
 284 nents. The equality in absolute terms of the coefficients in Column 3 shows that both ex-
 285 tremes of the max–min range account for the bulk of the variance in overall uncertainty:
 286 a deterioration in $s_{min,f}^e$ or an equally sized improvement in the $s_{max,f}^e$ symmetrically in-
 287 crease the max–min range.⁹ Columns 4 and 5 show that $s_{min,f}^e$ and $s_{max,f}^e$ proxy for down-
 288 side ($St.Dev.Down_f$) and upside uncertainty ($St.Dev.Up_f$), respectively. We define down-
 289 side (upside) uncertainty as the part of the variance accounted by outcomes below (above)
 290 mean so that $Std.Dev^2 = Std.Dev.Down^2 + Std.Dev.Up^2$. $Std.Dev.Down^2$ is equal to $\sum_{i=1}^I p_{i,f}$
 291 $\times (s_{i,f}^e - s_{avg,f}^e)^2 \times (s_{i,f}^e \leq s_{avg,f}^e)$ and $Std.Dev.Up^2$ is equal to $\sum_{i=1}^I p_{i,f} \times (s_{i,f}^e - s_{avg,f}^e)^2 \times$
 292 $(s_{i,f}^e > s_{avg,f}^e)$, where $p_{i,f}$ represents the subjective probability that each firm f attaches to
 293 a specific sales interval i , $s_{i,f}^e$ is the mid-point of each interval; s_{avg}^e denotes the first mo-
 294 ment of the subjective distribution of future sales calculated as $s_{avg,f}^e = \sum_{i=1}^I p_{i,f} \times s_{i,f}^e$; and
 295 $(s_{i,f}^e \leq s_{avg,f}^e)$ is an indicator equal to one when the condition in brackets is verified.

296 Results in Column 4 indicate that $s_{min,f}^e$ is the main determinant of downside uncertainty:
 297 a lower $s_{min,f}^e$ increases downside uncertainty about four times more than an equally-sized
 298 deterioration in $s_{max,f}^e$. By the same logic, Column 5 shows that $s_{max,f}^e$ is the main deter-

⁹The equality in absolute terms of the estimated coefficients mirrors the results from the variance decompo-
 sition of $\sigma_{max-min,f,t}$ into $s_{min,f,t}^e$ and $s_{max,f,t}^e$. After computing a standard variance decomposition using data
 for every firm, we pool the results to construct the unconditional distribution across firms. For every firm f ,
 we compute the shares of the variance attributed to $s_{max,f,t}^e$ and $s_{min,f,t}^e$ as $\beta_{cov,s_{min,f,t}^e} \equiv \frac{cov(s_{min,f,t}^e, \sigma_{max-min,f,t})}{var(\sigma_{max-min,f,t})}$ and

$$\beta_{cov,s_{max,f,t}^e} \equiv \frac{cov(s_{max,f,t}^e, \sigma_{max-min,f,t})}{var(\sigma_{max-min,f,t})}.$$

299 minant of upside uncertainty. As the specifications in Columns 4 and 5 include the mean
300 of expected future sales $s_{avg,f}^e$, our results are not driven by the indirect effect of $s_{min,f}^e$ and
301 $s_{max,f}^e$ on the mean $s_{avg,f}^e$.

302 3.2 Firm-Level Uncertainty Varies by Age, Size, and Sector

303 Our measure of firm-level uncertainty has three advantages. First, $\sigma_{max-min,f,t}$ is an
304 ex ante measure of the uncertainty perceived by firms about future outcomes. Second,
305 $\sigma_{max-min,f,t}$ reflects the managers' expectations—that is, the decision makers of the firm.
306 Third, $\sigma_{max-min,f,t}$ can be easily interpreted as it relates to economic outcomes.

307 In our sample, uncertainty around managers' average expected future sales is 9.81 per-
308 centage points; the median uncertainty is instead 8. $\sigma_{max-min,f,t}$ is virtually acyclical with
309 a correlation with the contemporaneous growth rate of real GDP of negative 0.07 (negative
310 0.03 and 0.00 with the first lag and the first lead of real GDP, respectively). This result reflects
311 the similar comovement of $s_{min,f,t}^e$ and $s_{max,f,t}^e$ with contemporaneous economic activity.

312 The data indicate that firms' uncertainty correlates with firms' characteristics such as
313 age, size, and the sector in which they operate. As shown in the first column of Figure 1,
314 uncertainty is negatively correlated with size and age. Young firms (less than five years) and
315 small and medium-sized firms (defined here as having less than 50 employees), on average,
316 perceive a higher level of uncertainty (13 percentage points). Interestingly, $\sigma_{max-min,f,t}$ is
317 acyclical, except for young firms and small and medium-sized firms that display a negative
318 correlation with real GDP equal to negative 0.11 and negative 0.22, respectively.

319 As shown in the middle and right columns of Figure 1, the extremes of the max–min
320 range, $s_{max,f,t}^e$ and $s_{min,f,t}^e$, display different correlations with size and age. $s_{max,f,t}^e$ is nega-
321 tively correlated with size and age, with $s_{max,f,t}^e$ lower for older and small firms. Young firms
322 expect, on average, a higher growth rate in the best-case scenario, $s_{max,f,t}^e$. The sales growth
323 rate in the worst-case scenario is instead negatively correlated with size and positively cor-

324 related with age.

325 The max–min range reported by large firms is about 50 percent less than the uncertainty
326 perceived by smaller and medium firms, consistent with life-cycle dynamics suggesting that
327 they have already reached their optimal size or achieved a better knowledge of the market
328 in which they operate. Finally, firms in the service sector face, on average, a similar level
329 of uncertainty with those in the manufacturing sector. Old firms (with age equal to more
330 than five years) and manufacturing firms drive the full sample results as they account for a
331 significant fraction of it. We refer the reader to Table A.2 in Appendix C for the full set of
332 descriptive statistics.

333 3.3 Covariates of Firm-Level Uncertainty

334 This section analyzes more formally whether measures of uncertainty correlate with past
335 and future business prospects as well as past forecast errors. We focus on this specific sub-
336 set of variables to connect our work with other studies in the literature; see, for instance,
337 Bachmann et al. (2018) and Altig et al. (2022). Toward this goal, we regress $s_{min,f,t}^e$, $s_{max,f,t}^e$
338 and $\sigma_{max-min,f,t}$ on measures of past and future business prospects for the firm (proxied by
339 the realized growth rate of sales $\Delta Sales_{t-1,t-2}$ and $s_{avg,f,t}^e$, respectively) as well as on firm's
340 past forecast errors, controlling for the firm's number of employees, cohort effects (age of
341 the firm), and firm-specific, industry, and year effects. Table 3 reports our estimates.

342 Starting from future business conditions, we find a positive correlation between the av-
343 erage expected growth rate of sales ($s_{avg,f,t}^e$) and firm-level uncertainty ($\sigma_{max-min,f,t}$). This re-
344 sult indicates that, at the firm level, fluctuations in uncertainty are positively correlated with
345 movements in the mean of the probability distribution of expected outcomes. As shown in
346 Columns 2 and 3, the positive correlation results from $s_{max,f,t}^e$ being more correlated to $s_{avg,f,t}^e$
347 than $s_{min,f,t}^e$.

348 Perceived uncertainty increases with firms' past forecast errors: a standard deviation in-

crease in *Abs.Forec.Error* predicts larger firm's uncertainty by about one half of a percentage point. As shown in Columns 2 and 3, larger forecast errors prompt firms to widen the range of expected outcomes, reducing $s_{min,f,t}^e$ and increasing $s_{max,f,t}^e$. In a separate regression (not shown), we also regress future forecast errors on current uncertainty, finding a positive and significant relationship (0.23 with a p-value lower than 0.01), suggesting that higher uncertainty ex ante predicted realized risk ex post.¹⁰

We also analyze the impact of past realized sales growth on uncertainty and expectations. Following the approach in [Bachmann et al. \(2018\)](#), we let the relationship between past sales growth and uncertainty to be nonmonotonic, allowing coefficients on past sales growth to differ between past episodes of positive ($\Delta Sales_{f,t-1} > 0$) and negative ($\Delta Sales_{f,t-1} \leq 0$) realized sales growth. Our estimates indicate that there is an asymmetric V-shape relationship between uncertainty and past sales, in line with results in [Bachmann et al. \(2018\)](#) and [Altig et al. \(2022\)](#). Uncertainty is more responsive to negative sales than positive ones by a factor of five, with the latter close to but not statistically significant. A one standard deviation reduction to a negative growth rate of sales is associated with an increase in $\sigma_{max-min,f,t}$ equal to one half of a percentage point. The lack of significance of positive sales on $\sigma_{max-min,f,t}$ stems from not significant correlation between $s_{min,f,t}^e$ and past positive sales. $s_{max,f,t}^e$ increases with more positive sales and more negative sales rising, ceteris paribus, $\sigma_{max-min,f,t}$. Instead, $s_{min,f,t}^e$ becomes more negative only with more negative sales, creating the one-sided response of $\sigma_{max-min,f,t}$ to negative sales.

As shown by the R^2 of 0.44 in Column 1, more than half of the variance of firm-level uncertainty $\sigma_{max-min,f,t}$ is unexplained and not accounted for by firm-specific observables or sector-specific or aggregate factors.

¹⁰Our specification controls for firm-specific effects as well as sectoral and year dummies.

372 **3.4 Firm-Level Uncertainty Persists for a Few Years**

373 We now turn to study the persistence of firm-level uncertainty. Our analysis's main take-
374 away is that, on average, firm-level uncertainty does not abate quickly but lasts for a few
375 years. To establish this result, we fit an autoregressive process of order one to $\sigma_{max-min,f,t}$,
376 $s_{min,f,t}^e$ and $s_{max,f,t}^e$, and exploit the 2017 wave of INVIND that elicits the full probability dis-
377 tribution of expected sales one year and three years ahead. This strategy allows us to study
378 how uncertainty about sales growth in 2020 evolved from 2017 to 2019, using the max-min
379 range of three years and one year ahead.

380 Fitting an autoregressive process of order one to $\sigma_{max-min,f,t}$ yields an estimated coeffi-
381 cient of 0.38 (statistically significant at 1 percent). As estimating persistence in a panel with
382 a limited number of periods results in biased-down estimates of persistence, see [Nickell](#)
383 (1981), we interpret this estimate as a lower bound.

384 Regressing the one year ahead max-min range in 2019 on the three year ahead max-min
385 range in 2017 yields a coefficient of 0.54 (statistically significant at 5 percent), implying an
386 autoregressive coefficient of roughly 0.74 ($0.54^{1/2}$). This strategy provides a clean test of the
387 persistence of uncertainty, but, at the same time, the evidence is obtained for a specific time
388 period. To be conservative, we interpret 0.74 as an upper bound of the persistence of the
389 max-min range.

390 In light of our considerations on the strengths of each approach, we consider 0.56, the
391 mid-point of our estimates, as the best estimate and conclude that uncertainty is a persistent
392 process that does not abate quickly with the half-life of a shock to be about one and a half
393 years. Results are similar for downside and upside uncertainty.

394 We estimate an autoregressive coefficient of 0.31 for $s_{max,f,t}^e$ and 0.27 for $s_{min,f,t}^e$. Instead,
395 looking at three-year uncertainty, we estimate a coefficient of 0.71 (statistically significant at
396 5 percent) yielding an implied autoregressive coefficient of about 0.8 for downside uncer-

397 tainty. The same estimates for upside uncertainty yield an estimate coefficient of 0.54 (sta-
 398 tistically significant at 10 percent) and an implied autoregressive coefficient of about 0.74.
 399 $s_{min,f,t}^e$ and $s_{max,f,t}^e$ on average, display a persistence similar to the max-min range. In short,
 400 our estimates indicate that uncertainty and its components persist for a few years.

401 **4 Measuring the Effects of Firm-Level Uncertainty**

402 We now study the economic effects of uncertainty by tracing the dynamic responses of
 403 a large set of real and financial variables, broadening the analysis's scope relative to most
 404 of the existing literature. In Section 4.1, we describe in detail our empirical approach. In
 405 Section 4.2, we show that fluctuations in uncertainty are associated with sizable effects not
 406 only on investment but also on labor variables and cash holdings.

407 **4.1 Empirical Methodology**

408 To estimate the economic effects of fluctuations in uncertainty our strategy relies on the
 409 local projection technique, discussed in Jordà (2005). To trace the dynamic economic effects
 410 of uncertainty fluctuations over a broad range of outcomes we project firm-level real and
 411 financial variables at different horizons on contemporaneous uncertainty $\sigma_{max-min,f,t}$ and its
 412 components $s_{min,f,t}^e$ and $s_{max,f,t}^e$ while controlling for potentially confounding factors shown
 413 as

$$Y_{f,t+h} = \sum_{f=1}^F \alpha_{f,h} + \beta_{max-min,h} \times \sigma_{max-min,f,t} + \sum_{s=1}^S \eta_{s,h} \text{Controls}_{s,t} + \epsilon_{f,t+h}; \quad (1)$$

414 and,

$$Y_{f,t+h} = \sum_{f=1}^F \alpha_{f,h} + \beta_{min,h} \times s_{min,f,t}^e + \beta_{max,h} \times s_{max,f,t}^e + \sum_{s=1}^S \eta_{s,h} \times \text{Controls}_{s,t} + \epsilon_{f,t+h}; \quad (2)$$

for $h = 0 \dots 4$,

415 where $Y_{f,t+h}$ includes the set of real and financial outcomes: the log of investment, the
416 log of total hours (distinguishing between the number of workers and hours-per-worker),
417 the capacity utilization rate, and the growth rate of liquid assets, or cash, held by the firm.

418 The coefficient $\beta_{max-min,h}$ measures the economic effects of overall uncertainty, while
419 $\beta_{min,h}$ and $\beta_{max,h}$ quantify the role of each component. To tease out confounding firm-level,
420 sectoral, or aggregate factors, Equations 1 and 2 include a set of controls. To isolate fluctua-
421 tions in uncertainty from correlated changes in current or *future* business conditions, the set
422 of $Controls_{s,t}$ includes the growth rate of sales realized at time t ($\Delta Sales_{f,t}$) and the expected
423 growth rate of sales one year ahead ($s_{avg,f,t}^e$). Observing $s_{avg,f,t}^e$ allows us to control for fore-
424 cast errors, or "sales surprises" defined as the difference between the growth rate of sales
425 at time t expected at time $t-1$ ($s_{avg,f,t-1}^e$) and the sales realized at time t . To account for the
426 impact of financial factors on firm's hiring and investment decisions, we also include book
427 leverage at time $t-1$.

428 The panel structure of our data allows us to control for time-invariant factors specific to
429 each firm, $\alpha_{f,h}$, ruling out that our results are driven by the correlation between the mean of
430 $\sigma_{max-min,f,t}$ and the ones of dependent variables. Finally, the set of $Controls$ features sector,
431 and year dummies to account for unobserved industry-specific characteristics or aggregate
432 factors, potentially related to policy changes or business cycle fluctuations. In sum, to es-
433 timate the economic effects of uncertainty we exploit fluctuations of real and financial out-
434 comes around firm- and sector-specific means while simultaneously netting out common
435 movements of uncertainty across firms (through time effects).

436 4.2 Real and Financial Effects of Uncertainty

437 Our findings indicate that the economic effects of uncertainty are not limited to invest-
438 ment but extend to the labor market and the firm's financial structure. Table 4 reports the
439 dynamic response of firm-level variables following a 1 percentage point increase in firm-

440 level uncertainty. Entries are expressed in percent.

441 Fluctuations in uncertainty predict economic effects that are statistically and economi-
442 cally significant. Notably, these effects do not abate quickly and last for a few years. This
443 result reflects both the persistence of firms' perceived changes in uncertainty (as shown in
444 Section 3.4) and the sluggishness of firms' endogenous responses that first adjust soft mar-
445 gins like labor and only then change investment. On impact, firms also increase their cash
446 holdings, signaling a precautionary behavior that anticipates reducing investment. We dis-
447 cuss these results in turn.

448 On the real side, after an increase in perceived uncertainty equal to one standard devia-
449 tion (5.63 is the standard deviation of $\sigma_{max-min,f,t}$ for the median firm), the firm reduces its
450 capacity utilization rate and total hours by about 0.5 and 0.8 percent, respectively, equiva-
451 lent to about 70 percent of one standard deviation of both variables. Also, a reduction in
452 employed workers, smaller than that of hours, signals that the intensive margin of labor
453 is adjusted more swiftly. Over the same period, on the financial side, firms also increase
454 the growth rate of cash holdings, before reverting in year 2. After one year, the firm starts
455 cutting on investment, by more than 2 percent in each of the following two years (or about
456 one investment standard deviation). As the increase in uncertainty is reabsorbed, invest-
457 ment overshoots its steady-state level before converging, but the effect is not statistically
458 significant.

459 To gauge the magnitude of the estimated effects it is instructive to compare our results
460 with existing studies that create measures of uncertainty (or risk) at the firm level. We es-
461 timate the cumulative effects of uncertainty are larger than what we typically found in the
462 existing literature and play out at longer horizons. A study similar to our work is [Alfaro](#)
463 [et al. \(2017\)](#), which employs measures of financial volatility to proxy for firm-level uncer-
464 tainty in the United States and studies its effect one year out on investment, employment,

465 and cash holdings. Relative to [Alfaro et al. \(2017\)](#), the effects of uncertainty are twice as
466 large one year out, while employment is comparable with total hours in magnitude, consis-
467 tent with the intensive margin being more important in European labor markets than in the
468 United States. The response of cash holdings in our sample is about half of their estimates.
469 Overall, the cumulative effects on real activity are larger given our focus at longer horizons.
470 Larger estimated effects are found also relative to studies that employ textual analysis to
471 disentangle sources of uncertainty, or risk, such as political risk in [Hassan et al. \(2019\)](#) and
472 in [Caldara et al. \(2020\)](#) for trade policy uncertainty.¹¹

473 5 Effects of Uncertainty through "Downside Uncertainty"

474 We now study whether the economic effects of uncertainty depend on the source driving
475 the increase in dispersion of future expected sales—that is, whether it comes from downside
476 or upside uncertainty. Typically, the existing literature does not distinguish between the
477 source of fluctuations in uncertainty, mostly because of the limitation imposed by existing
478 data.¹² Understanding this issue is important for at least two reasons. From an empirical
479 standpoint, the source of the increase in uncertainty may predict its economic effects. For
480 instance, higher uncertainty may display sizable economic effects only if driven by disper-
481 sion in positive or upside (negative or downside) outcomes. From a theoretical standpoint,
482 measuring the effects of downside and upside uncertainty provides overidentifying restric-
483 tions against which to test competing models aimed at quantifying the aggregate effects of
484 uncertainty. (We return to this issue in Section 6.) To quantify the economic effects of down-
485 side and upside uncertainty, we estimate Equation 2 that relaxes the implicit assumption
486 imposed in Section 4.2 that forced the coefficients of $s_{max,f,t}^e$ and $s_{min,f,t}^e$ to be the same in

¹¹In [Caldara et al. \(2020\)](#) investment drops about one and a half percent for a year, about three times as much as the contemporaneous drop in [Hassan et al. \(2019\)](#) due to political risk.

¹²[Segal et al. \(2015\)](#) constitute an important exception. They study the role of downside and upside (or bad and good) uncertainty for aggregate macroeconomic series and financial markets, finding that both matter.

487 absolute terms.

488 The main takeaway is that firms respond to fluctuations in uncertainty only if it orig-
489 inates with downside uncertainty. Table 5 reports the full set of estimates. Our findings
490 indicate that only an increase in downside uncertainty induces negative economic effects.
491 Instead, an increase in upside uncertainty does not result in statistically significant economic
492 effects (except for total hours). The propagation mechanism of fluctuations in downside un-
493 certainty (or equivalently an increase in uncertainty driven by a deterioration in the worst-
494 case scenario) is similar to the one discussed in Section 4.2. As shown in Figure 2, which
495 reports the impulse responses following an increase in overall and downside uncertainty
496 with associated 90 percent confidence bands, firms first reduce capacity utilization and total
497 hours and then investment.¹³ Over time, as the initial effect of the shock wanes, the dynam-
498 ics are reverted. From a quantitative standpoint, the effects of uncertainty are somewhat
499 larger than the one of overall uncertainty, especially for investment.

500 Disentangling the individual contribution of upside and downside uncertainty sheds
501 light on the dynamics induced by an increase in $\sigma_{max-min,f,t}$. The estimated effects of an
502 increase in uncertainty confound the significant sensitivity of firms' decisions to the rise in
503 downside uncertainty and its unresponsiveness to upside uncertainty. Dynamics associated
504 with fluctuations in downside uncertainty are statistically and economically significant. As
505 shown in Appendix D, our results are robust when downside uncertainty is proxied by
506 $s_{avg,f,t}^e - s_{min,f,t}^e$ and upside uncertainty by $s_{max,f,t}^e - s_{avg,f,t}^e$.

507 6 Implications for Macroeconomic Modeling

508 Firm-level uncertainty results in a persistent drop in employment, hours per worker,
509 capital as well as an increase in cash holdings only when it originates from downside uncer-

¹³As the standard deviation of $\sigma_{max-min,f,t}$ and $s_{min,f,t}^e$ is similar (5.63 and 6.15, respectively), we pick the same shock equal to 5.63 for total and downside uncertainty to highlight the differences in the estimated coefficients.

510 tainty. While most of the existing literature has focused on investment, the immediate and
511 persistent drop in hours in response to higher uncertainty suggests that labor behaves more
512 like a durable input similar to capital rather than being determined purely by contempo-
513 raneous considerations. How does our evidence discipline existing theories of uncertainty,
514 and what are the implications for macroeconomic models? To reproduce the negative effects
515 of uncertainty, macroeconomic frameworks rely on models of "real options" or models that
516 emphasize financial frictions, or models featuring robust control and ambiguity aversion.¹⁴

517 To obtain the negative effects both on capital and employment as well as cash hoarding,
518 theories of real options emphasize "wait and see" motives because of the presence of ad-
519 justment costs that give firms the option to delay investment and hiring in the presence of
520 uncertainty and make reversing decisions costly; see, for instance, [Alfaro et al. \(2017\)](#). With
521 input irreversibility due to firm specificity or the absence of secondary markets, Bernanke's
522 Bad News Principle applies with firms responding only to fluctuations in downside uncer-
523 tainty. This choice increases firm's profits in low future productivity states in which the
524 irreversibility constraint is binding and the firm cannot downsize capital or employment.
525 More generally, our evidence supports theories of real options delivering an asymmetric
526 adjustment cost function, in which downsizing capital or employment is costly.

527 Another approach in the literature emphasizes financial considerations with higher down-
528 side uncertainty about future sales potentially increasing the firm's likelihood of facing fi-
529 nancial constraints, leading to a drop in investment and hiring. In [Christiano et al. \(2014\)](#)
530 and [Chugh \(2016\)](#), an increase in risk about the realizations of idiosyncratic productivity in
531 converting raw to productive capital results in lower credit extended to firms, that, in turn,
532 acquire less capital and labor.

¹⁴On theoretical grounds, it is well known that the economic effects of uncertainty are, in general, ambiguous and depend on the assumptions about the production technology, competition in product markets, the shape of adjustment costs, and management attitudes toward uncertainty. Uncertainty can potentially have positive effects; see, for instance, the discussion in [Guiso and Parigi \(1999\)](#) and [Bloom \(2014\)](#).

533 Another strand of the literature emphasizes robust control and ambiguity aversion in
534 [Hansen et al. \(1999\)](#), [Ilut and Schneider \(2014\)](#), and [Ilut and Saijo \(2021\)](#), where the negative
535 effects of uncertainty are driven by loss of confidence about future outcomes. Ambiguity
536 averse agents act as if they evaluate plans using a worst case probability drawn from a set
537 of multiple beliefs. A loss of confidence makes the “worst case” mean worse, and agents act
538 as if they have received bad news about the future prompting them to substitute away from
539 uncertainty and reducing current hours worked. Assuming that the minimum of future
540 sales is a summary statistic for the probability distribution under the worst-case scenario,
541 our evidence is also consistent with this class of models as agents respond to a deterioration
542 in the worst-case scenario while being insensitive to improvements in the best-case scenario.
543 Confidence as a driver of fluctuations with shocks driving “wedges” in beliefs is also the
544 focus of [Angeletos et al. \(2018\)](#) and [Angeletos and Lian \(2021\)](#).

545 **7 A New Measure of Aggregate Uncertainty**

546 We now construct an economy-wide measure of uncertainty, denoted by $\sigma_{max-min,agg,t}$
547 based on an aggregation of the max–min range at the firm level. Aggregate uncertainty
548 $\sigma_{max-min,agg,t}$ is a summary statistic of total firm-level uncertainty perceived by each firm,
549 reflecting aggregate, sector- and firm-specific factors. Our bottom-up microeconomic ap-
550 proach provides a unicum in the literature, as it covers multiple business cycles. Similarly,
551 [Altig et al. \(2020\)](#) and [Altig et al. \(2022\)](#) use survey data to construct an aggregate proxy of
552 aggregate uncertainty. Still, data availability limits the length of their series extending (al-
553 beit a monthly rather than yearly frequency) to the past six years. Alternative strategies are
554 presented in [Bloom \(2009\)](#) and [Bloom et al. \(2018\)](#), which proxy aggregate uncertainty using
555 dispersion in realized outcomes, and in [Bachmann et al. \(2013\)](#), which construct uncertainty
556 measures based on both ex ante disagreement and ex post forecast error about future out-

557 comes. [Jurado et al. \(2015\)](#) adopted a latent-variable approach to extract a measure of the
558 common variation in uncertainty across more than 100 macroeconomic series.

559 Our aggregate measure, $\sigma_{max-min,agg,t}$, is constructed averaging firm-level uncertainty,
560 with the weight on each firm being the product between their sales and the statistical weight
561 representing the share of each firm in the entire population of firms. The mean and the stan-
562 dard deviation of $\sigma_{max-min,agg,t}$ are 8.53 and 1.60 percentage points, respectively. Similarly,
563 we construct a measure of the aggregate minimum $s_{min,agg,t}^e$ (mean -2.10 with a standard de-
564 viation of 3.25) and the aggregate maximum $s_{max,agg,t}^e$ (mean of 6.24 and a standard deviation
565 of 2.35). Unsurprisingly, the volatility of the series is smaller than its firm-level counterpart.
566 Unlike firm-level uncertainty, aggregate uncertainty is negatively correlated with real GDP
567 growth (-0.58), see [Table 6](#). The countercyclicality of $\sigma_{max-min,agg,t}$ results from compositional
568 effects with i) $\sigma_{max-min,f,t}$ being countercyclical for small and medium firms and ii) small and
569 medium firms' sales being less countercyclical than large firms. As a result, in bad times
570 the aggregate measure weighs more small and medium firms that, in turn, perceive higher
571 uncertainty. Both factors yield a countercyclical $\sigma_{max-min,agg,t}$. In addition, $\sigma_{max-min,agg,t}$ is
572 negatively correlated with $s_{agg,avg,t}^e$, an economy-wide measure of mean expectation about
573 future sales, constructed using the same weights. The aggregation of the minimum, denoted
574 by $s_{min,agg,t}^e$, and the aggregate maximum, denoted by $s_{max,agg,t}^e$, are strongly procyclical, with
575 a correlation with the growth rate of real GDP of 0.91 and 0.84, respectively. As the minimum
576 decreases, downside uncertainty rises.

577 While the countercyclicality of proxies of aggregate uncertainty is typically obtained in
578 the literature, we emphasize that the correlation of our measure of ex ante aggregate uncer-
579 tainty, $\sigma_{max-min,agg,t}$, with measures of cross-sectional dispersion of sales, hours, or capacity
580 utilization is close to zero or slightly negative.

581 As shown in [Section 3.3](#), firm-level ex ante uncertainty $\sigma_{max-min,f,t}$ is linked with real-

582 ized ex post uncertainty: $\sigma_{max-min,f,t}$ increases with larger past forecast errors and predicts
583 larger future forecast errors, validating that indeed the max–min range is connected with
584 realized ex post risk. The statistically significant link appears to be quantitatively tenuous:
585 an increase of a standard deviation in the forecast error is associated to an increase in the
586 max–min range equal to about one sixth of its standard deviation. Through the lens of this
587 metric, the lack of correlation between $\sigma_{max-min,agg,t}$ and measures of cross-sectional dis-
588 persion suggests that an increase in aggregate uncertainty does not necessarily lead to an
589 increase in cross-sectional dispersion and much of the variation in the cross-sectional prox-
590 ies is not driven by ex-ante uncertainty. Our evidence supports models in which shocks that
591 can generate responses to uncertainty that are not necessarily connected to later realized
592 changes in risk; see, for instance, [Ilut and Schneider \(2014\)](#) and [Angeletos et al. \(2018\)](#).

593 Figure 3 plots our measure $\sigma_{max-min,agg,t}$ together with the growth rate of real GDP. (The
594 series for aggregate $\sigma_{max-min,agg,t}$ is demeaned.) Excluding the current spike due to the
595 COVID-19 pandemic, uncertainty peaked in the 2009 Global Financial Crisis (GFC) and rose,
596 although to a lesser extent, in 2012 during the sovereign debt crisis (SDC). During the GFC
597 and SDC, uncertainty increased more in the manufacturing sector relative to the service sec-
598 tor. In contrast, in 2020 at the peak of the COVID-19 pandemic, uncertainty nearly doubled
599 in the service sector, and it increased by 50 percent in the manufacturing sector.

600 Beyond business cycle effects, our measure was also affected by political considerations
601 in 2019, reaching levels comparable with the SDC due to elevated political uncertainty. The
602 time-series profile of selected percentiles of the cross-sectional uncertainty distribution offers
603 more insight into what firms accounted for the increase in aggregate uncertainty. The GFC
604 increased uncertainty more for large firms. The average size of firms in the fourth quartile
605 (pool of high uncertainty, above the 75th percentile of uncertainty in a given year) reached
606 about 430 employees, a jump of 30 percent from 2008. Similarly, the political uncertainty in

607 2019, the average size in the pool of high uncertainty increased by 50 percent. In contrast, the
608 SDC appears to have affected more significantly smaller firms, a narrative in line with the
609 struggle of the banking sector to cope with the crisis of sovereign debt and provide credit to
610 smaller firms. Compositional effects did not play a role during Covid-19 as the distribution
611 shifted with tiny changes in average size across quartiles.

612 **8 Final Remarks**

613 We study the economic effects of time-varying uncertainty and offer a unique perspective
614 that addresses some of the most pressing measurement issues regarding uncertainty at the
615 firm-level. Access to microeconomic data allows us to construct, for a representative panel of
616 firms, a measure of subjective ex ante uncertainty based on business managers' expectations
617 that span over two decades and multiple business cycle episodes.

618 We document the properties of time-varying uncertainty across firms' size, age, and sec-
619 tors, showing that firm-level uncertainty is a persistent process. Our empirical analysis de-
620 tails the propagation mechanism of uncertainty fluctuations at the firm level showing that
621 they induce long-lasting economic effects across various real and financial variables only
622 when driven by an increase in the downside component of uncertainty. In this sense, not all
623 uncertainties are alike, and the source of uncertainty matters, with only its downside com-
624 ponent resulting in meaningful economic effects. Our evidence provides a practical set of
625 overidentifying restrictions against which to test competing macroeconomic models.

626 We construct a bottom-up measure of ex ante aggregate uncertainty. The lack of correla-
627 tion between our bottom-up proxy and measures of cross-sectional dispersion suggest that
628 much of the variation in cross-sectional dispersion is not driven by uncertainty. At the ag-
629 gregate level, our results support modelling of uncertainty in which an increase in perceived
630 uncertainty is not necessarily connected to later realized changes in risk.

References

- 631
632 Alfaro, I., Bloom, N., Lin, X., 2017. The Finance-Uncertainty Multiplier. Mimeo .
- 633 Altig, D., Baker, S., Barrero, J.M., Bloom, N., Bunn, P., Chen, S., Davis, S.J., Leather, J., Meyer,
634 B., Mihaylov, E., Mizen, P., Parker, N.a., 2020. Economic uncertainty before and during the
635 COVID-19 pandemic. *Journal of Public Economics* 191.
- 636 Altig, D., Barrero, J.M., Bloom, N., Davis, S.J., Meyer, B., Parker, N., 2022. Surveying business
637 uncertainty. *Journal of Econometrics* 231, 282–303. *Annals Issue: Subjective Expectations*
638 *& Probabilities in Economics*.
- 639 Angeletos, G., Collard, F., Dellas, H., 2018. Quantifying Confidence. *Econometrica* 86, 1689–
640 1726.
- 641 Angeletos, G.M., Lian, C., 2021. Confidence and the Propagation of Demand Shocks. *The*
642 *Review of Economic Studies* 89, 1085–1119.
- 643 Armantier, O., de Bruin, W.B., Topa, G., Klaauw, W., Zafar, B., 2015. Inflation Expectations
644 and Behavior: Do Survey Respondents Act on Their Beliefs? *International Economic*
645 *Review* 56, 505–536.
- 646 Bachmann, R., Carstensen, K., Lautenbacher, S., Schneider, M., 2018. Uncertainty and
647 Change: Survey Evidence of Firms' Subjective Beliefs. Working Paper .
- 648 Bachmann, R., Carstensen, K., Lautenbacher, S., Schneider, M., 2020. Uncertainty Is More
649 Than Risk – Survey Evidence on Knightian and Bayesian Firms. Working Paper .
- 650 Bachmann, R., Elstner, S., Hristov, A., 2017. Surprise, surprise—measuring firm-level invest-
651 ment innovations. *Journal of Economic Dynamics and Control* 83, 107–148.
- 652 Bachmann, R., Elstner, S., Sims, E.R., 2013. Uncertainty and Economic Activity: Evidence
653 from Business Survey Data. *American Economic Journal: Macroeconomics* 5, 217–249.
- 654 Baker, S.R., Bloom, N., Davis, S.J., 2016. Measuring economic policy uncertainty. *The Quar-*
655 *terly Journal of Economics* 131, 1593–1636.
- 656 Ben-David, I., Graham, J.R., 2013. Managerial Miscalibration. *The Quarterly Journal of*
657 *Economics* 128, 1547–1584.
- 658 Bernanke, B.S., 1983. Irreversibility, Uncertainty, and Cyclical Investment. *The Quarterly*
659 *Journal of Economics* 98, 85–106.
- 660 Bloom, N., 2009. The Impact of Uncertainty Shocks. *Econometrica* 77, 623–685.
- 661 Bloom, N., 2014. Fluctuations in uncertainty. *Journal of Economic Perspectives* 28, 153–76.
- 662 Bloom, N., Bond, S., Van Reenen, J., 2007. Uncertainty and investment dynamics. *The*
663 *Review of Economic Studies* 74, 391–415.
- 664 Bloom, N., Floetotto, M., Jaimovich, N., Saporta-Eksten, I., Terry, S.J., 2018. Really Uncertain
665 Business Cycles. *Econometrica* 86, 1031–1065.

- 666 Bontempi, M.E., Golinelli, R., Parigi, G., 2010. Why demand uncertainty curbs investment:
667 Evidence from a panel of italian manufacturing firms. *Journal of Macroeconomics* 32,
668 218–238.
- 669 Caldara, D., Iacoviello, M., Molligo, P., Prestipino, A., Raffo, A., 2020. The economic effects
670 of trade policy uncertainty. *Journal of Monetary Economics* 109, 38 – 59. Special Issue:
671 April 2019 Carnegie-Rochester-NYU Conference.
- 672 Christiano, L.J., Motto, R., Rostagno, M., 2014. Risk Shocks. *American Economic Review*
673 104, 27–65.
- 674 Chugh, S.K., 2016. Firm risk and leverage-based business cycles. *Review of Economic Dy-*
675 *namics* 20, 111–131.
- 676 Datta, D., Londono, J.M., Sun, B., Beltran, D.O., Ferreira, T.T., Iacoviello, M., Jahan-Parvar,
677 M., Li, C., Rodriguez, M., Rogers, J.H., 2017. Taxonomy of Global Risk, Uncertainty, and
678 Volatility Measures. *International Finance Discussion Papers*. Board of Governors of the
679 Federal Reserve System (U.S.).
- 680 Dominitz, J., Manski, C.F., 1994. Using Expectations Data to Study Subjective Income Ex-
681 pectations. NBER Working Papers 4937. National Bureau of Economic Research, Inc.
- 682 Dominitz, J., Manski, C.F., 2004. How Should We Measure Consumer Confidence? *Journal*
683 *of Economic Perspectives* 18, 51–66.
- 684 Fernández-Villaverde, J., Guerrón-Quintana, P.A., 2020. Uncertainty shocks and business cy-
685 cle research. *Review of Economic Dynamics* 37, S118–S146. The Twenty-Fifth Anniversary
686 of “Frontiers of Business Cycle Research”.
- 687 Gennaioli, N., Ma, Y., Shleifer, A., 2016. Expectations and Investment. *NBER Macroeco-*
688 *nomics Annual* 30, 379–431.
- 689 Guiso, L., Jappelli, T., Pistaferri, L., 2002. An Empirical Analysis of Earnings and Employ-
690 ment Risk. *Journal of Business & Economic Statistics* 20, 241–253.
- 691 Guiso, L., Jappelli, T., Terlizzese, D., 1992. Earnings Uncertainty and Precautionary Saving.
692 *Journal of Monetary Economics* 30, 307–337.
- 693 Guiso, L., Parigi, G., 1999. Investment and demand uncertainty. *The Quarterly Journal of*
694 *Economics* 114, 185–227.
- 695 Gulen, H., Ion, M., 2016. Policy uncertainty and corporate investment. *The Review of Fi-*
696 *nancial Studies* 29, 523–564.
- 697 Handley, K., Limão, N., 2017. Policy Uncertainty, Trade, and Welfare: Theory and Evidence
698 for China and the United States. *American Economic Review* 107, 2731–2783.
- 699 Hansen, L.P., Sargent, T.J., Tallarini, T.D., 1999. Robust Permanent Income and Pricing. *Re-*
700 *view of Economic Studies* 66, 873–907.

- 701 Hassan, T.A., Hollander, S., van Lent, L., Tahoun, A., 2019. Firm-Level Political Risk: Mea-
702 surement and Effects. *The Quarterly Journal of Economics* 134, 2135–2202.
- 703 Holzmeister, F., Huber, J., Kirchler, M., Lindner, F., Weitzel, U., Zeisberger, S., 2020. What
704 Drives Risk Perception? A Global Survey with Financial Professionals and Laypeople.
705 *Management Science* 66, 3977–4002.
- 706 Hurd, M.D., McGarry, K., 2002. The Predictive Validity of Subjective Probabilities of Sur-
707 vival. *Economic Journal* 112, 966–985.
- 708 Ilut, C., Saijo, H., 2021. Learning, confidence, and business cycles. *Journal of Monetary*
709 *Economics* 117, 354–376.
- 710 Ilut, C.L., Schneider, M., 2014. Ambiguous business cycles. *American Economic Review* 104,
711 2368–99.
- 712 Jordà, O., 2005. Estimation and Inference of Impulse Responses by Local Projections. *Ameri-*
713 *can Economic Review* 95, 161–182.
- 714 Jurado, K., Ludvigson, S.C., Ng, S., 2015. Measuring uncertainty. *American Economic Re-*
715 *view* 105, 1177–1216.
- 716 Kehrig, M., 2015. The cyclical nature of the productivity distribution. US Census Bureau
717 Center for Economic Studies Paper No. CES-WP-11-15 .
- 718 Leahy, J.V., Whited, T.M., 1996. The Effect of Uncertainty on Investment: Some Stylized
719 Facts. *Journal of Money, Credit and Banking* 28, 64–83.
- 720 Massenet, B., Pettinicchi, Y., 2018. Can firms see into the future? survey evidence from
721 germany. *Journal of Economic Behavior & Organization* 145, 66 – 79.
- 722 Morikawa, M., 2013. What Type of Policy Uncertainty Matters for Business? Technical
723 Report. Research Institute of Economy, Trade and Industry (RIETI).
- 724 Nickell, S.J., 1981. Biases in Dynamic Models with Fixed Effects. *Econometrica* 49, 1417–
725 1426.
- 726 Segal, G., Shaliastovich, I., Yaron, A., 2015. Good and bad uncertainty: Macroeconomic and
727 financial market implications. *Journal of Financial Economics* 117, 369 – 397.
- 728 Senga, T., 2015. A New Look at Uncertainty Shocks: Imperfect Information and Misalloca-
729 tion. Technical Report. Working Paper.
- 730 Stein, L.C., Stone, E., 2013. The effect of uncertainty on investment, hiring, and r&d: Causal
731 evidence from equity options. Working Paper .

Table 1: Firm-Level Expectations: Descriptive Statistics

	No. of Obs.	Mean	Std. Dev.	P_{10}	P_{25}	P_{50}	P_{75}	P_{90}	Corr w. $\Delta GDP_{t,t-1}$
$s_{avg,f,t}^e$	49674	3.56	11.30	-7.20	0.00	2.60	7.20	14.30	0.25
$s_{min,f,t}^e$	30958	-3.89	9.91	-12.00	-10.00	-2.00	1.00	5.00	0.28
$s_{max,f,t}^e$	30976	7.07	9.82	0.00	2.00	5.00	12.00	15.00	0.18
$\Delta Sales_{t,t-1}$	41934	0.93	18.70	-19.90	-7.51	1.76	10.40	21.10	0.28

Note: Statistics are computed over the sample period from 1996 to 2019, taking into account the INVIND sample weight represented by each firm in the entire population of firms. The number of observations refers to the number of firms effectively sampled in the data. Table entries are computed over growth rates (expressed in percent). $s_{avg,f,t}^e$, $s_{min,f,t}^e$, $s_{max,f,t}^e$ denote the *average*, *minimum*, and *maximum* expected growth rates of sales one year ahead, respectively, while $\Delta Sales_{t,t-1}$ and $\Delta GDP_{t,t-1}$ reports the growth rate of *realized* sales and the growth rate of GDP between time t and $t-1$, respectively. P_X reports the X^{th} percentile of the distribution.

Table 2: $\sigma_{max-min}$ and Moments of the Subjective Probability Distribution

Year 2005 and 2017	$St.Dev.f$ (1)	$Skew.f$ (2)	$St.Dev.f$ (3)	$St.Dev.Down_f$ (4)	$St.Dev.Up_f$ (5)
$\sigma_{max-min,f}$	0.28*** (0.00)	-0.25 (0.21)			
$s_{min,f}^e$			-0.28*** (0.00)	-0.30*** (0.00)	-0.09*** (0.00)
$s_{max,f}^e$			0.28*** (0.00)	0.08*** (0.00)	0.29*** (0.01)
R^2	0.84	0.00	0.84	0.83	0.84
Observations	2047	2047	2047	2047	2047

Note: Each equation is estimated with ordinary least squares using the 2005 and 2017 waves of IN-VIND. P-values are shown in parentheses. Stars denote significance level of the coefficient they refer to: * p-value<0.10, ** p value<0.05, *** p-value<0.01. The dependant variables are reported on columns. $St.Dev.f$ is the second moment and $Skew.f$ is the third-moment of the firm-specific probability distribution of expected sales for the year 2005 and 2017, respectively. $St.Dev.Down_f$ and $St.Dev.Up_f$ denote the downside and upside components of overall uncertainty, respectively. For every firm f , $\sigma_{max-min,f}$ denotes the difference between $s_{max,f}^e$ and $s_{min,f}^e$, the maximum and minimum expected growth rate of sales one year ahead.

Table 3: Uncertainty Covariates

	$\sigma_{max-min,f,t}$	$s_{min,f,t}^e$	$s_{max,f,t}^e$
	(1)	(2)	(3)
$s_{avg,f,t}^e$	0.09*** (0.00)	0.67*** (0.00)	0.76*** (0.00)
$Abs.Forec.Error_{f,t-1}$	0.04*** (0.00)	-0.02*** (0.00)	0.01** (0.01)
$\Delta Sales_{f,t-1} > 0$	0.01 (0.13)	0.00 (0.55)	0.02*** (0.00)
$\Delta Sales_{f,t-1} < 0$	-0.05*** (0.01)	0.02** (0.04)	-0.03*** (0.00)
Observations	7780	7784	7780
R^2	0.44	0.77	0.80

Note: Each regression is estimated by ordinary least squares over the sample period 1996 to 2019, and it also includes fixed effects, year- and industry-effects, and firms' age and size. $\sigma_{max-min,f,t}$ measures firm-level uncertainty; $s_{max,f,t}^e$, $s_{avg,f,t}^e$ and $s_{min,f,t}^e$ denote the maximum, average, and minimum one-year-ahead expected growth rates of sales, respectively.

Table 4: Real and Financial Effects of Firm-Level Uncertainty

Horizon=h	Increase in Uncertainty 1p.p.				
	0	1	2	3	4
<i>Capacity Util. (t+h)</i>	-0.096* (0.06)	-0.054* (0.09)	0.015 (0.77)	0.003 (0.97)	0.047 (0.22)
<i>Total Hours (t+h)</i>	-0.143*** (0.00)	-0.110** (0.05)	-0.063 (0.42)	-0.063 (0.41)	-0.013 (0.79)
<i>Hours-per-Worker (t+h)</i>	-0.088*** (0.00)	-0.025 (0.35)	-0.025 (0.39)	-0.051 (0.26)	0.001 (0.96)
<i>No. of Employees (t+h)</i>	-0.064 (0.11)	-0.093** (0.05)	-0.058 (0.11)	0.002 (0.95)	-0.029 (0.37)
<i>Real Investment (t+h)</i>	-0.039 (0.65)	-0.411* (0.10)	-0.524** (0.02)	0.201 (0.54)	0.443 (0.13)
<i>Growth Rate of Cash Holdings (t+h)</i>	0.011* (0.05)	-0.006 (0.22)	-0.008* (0.09)	0.000 (0.95)	-0.003 (0.62)

Note: The table reports ordinary least squares estimates of the coefficient β_h , the estimated coefficient on $\sigma_{max-min,f,t}$ in Equation 1. The sample period runs from 1996 to 2019. P-values are in parentheses. Stars denote the significance level of the coefficient they refer to: * p-value<0.10, ** p-value<0.05, and *** p-value<0.01. Standard errors are clustered by firm and year. Entries, except for cash holdings in percentage points, are expressed in percent.

Table 5: Real and Financial Effects of Firm-Level Uncertainty

Panel A - Increase in Downside Uncertainty 1p.p.					
Horizon=h	0	1	2	3	4
<i>Capacity Util. (t+h)</i>	-0.150*** (0.01)	-0.075** (0.01)	0.002 (0.95)	0.050 (0.40)	0.028 (0.67)
<i>Total Hours (t+h)</i>	-0.185*** (0.00)	-0.136** (0.01)	-0.108* (0.07)	-0.134** (0.03)	-0.038 (0.31)
<i>Hours-per-Worker (t+h)</i>	-0.088*** (0.00)	-0.025 (0.35)	-0.025 (0.39)	-0.051 (0.26)	0.001 (0.96)
<i>No. of Employees (t+h)</i>	-0.064 (0.11)	-0.093** (0.05)	-0.058 (0.11)	0.002 (0.95)	-0.029 (0.37)
<i>Real Investment (t+h)</i>	-0.099 (0.39)	-0.790** (0.02)	-0.594* (0.06)	-0.138 (0.73)	0.671** (0.06)
<i>Growth Rate of Cash Holdings (t+h)</i>	0.013** (0.02)	0.007 (0.35)	0.005 (0.25)	-0.010* (0.05)	0.001 (0.80)
Panel B - Increase in Upside Uncertainty 1 p.p.					
Horizon=h	0	1	2	3	4
<i>Capacity Util. (t+h)</i>	-0.029 (0.45)	-0.029 (0.63)	0.030 (0.68)	-0.051 (0.44)	0.073 (0.56)
<i>Total Hours (t+h)</i>	-0.095* (0.07)	-0.086 (0.18)	-0.024 (0.82)	0.015 (0.90)	0.012 (0.88)
<i>Hours-per-Worker (t+h)</i>	-0.005 (0.79)	0.013 (0.73)	-0.003 (0.85)	-0.029 (0.61)	0.005 (0.82)
<i>No. of Employees (t+h)</i>	-0.097 (0.21)	-0.088 (0.21)	-0.050 (0.53)	0.066 (0.31)	0.015 (0.81)
<i>Real Investment (t+h)</i>	0.034 (0.72)	0.007 (0.97)	-0.428 (0.21)	0.655 (0.23)	0.117 (0.37)
<i>Growth Rate of Cash Holdings (t+h)</i>	0.008 (0.14)	-0.005 (0.21)	-0.011 (0.11)	-0.010 (0.22)	-0.004 (0.65)

Note: The table reports ordinary least squares estimates of the coefficient $\beta_{min,h}$ in Panel A and $\beta_{max,h}$ in Panel B in Equation 2. The sample period runs from 1996 to 2019. P-values are in parentheses. Stars denote the significance level of the coefficient they refer to: * p-value<0.10, ** p-value<0.05, and *** p-value<0.01. Standard errors are clustered by firm and year. Entries, except for cash holdings in percentage points, are expressed in percent. Panel A reports the response of each variable to a 1 percentage point decrease in $s_{min,f,t}^e$ or equivalently an increase in downside uncertainty. Panel B reports the response of each variable to a 1 percentage point increase in $s_{max,f,t}^e$ or, equivalently, an increase in upside uncertainty.

Table 6: Correlation between Ex Ante and Ex Post Uncertainty Measures

Contemporaneous Correlation	$\Delta GDP_{t,t-1}$	$\sigma_{max-min,agg,t}$
$\sigma_{max-min,agg,t}$	-0.58	1
$S_{avg,agg,t}^e$	0.82	-0.51
<i>XS Sales dispersion_t</i>	-0.30	-0.14
<i>XS Empl. dispersion_t</i>	-0.21	0.10
<i>XS Cap. Util. dispersion_t</i>	-0.46	0.04

Note: Each entry reports the contemporaneous correlation between the growth rate of real GDP $\Delta GDP_{t,t-1}$ and ex ante uncertainty $\sigma_{max-min,agg,t}$. The sample period is from 1997 to 2021.

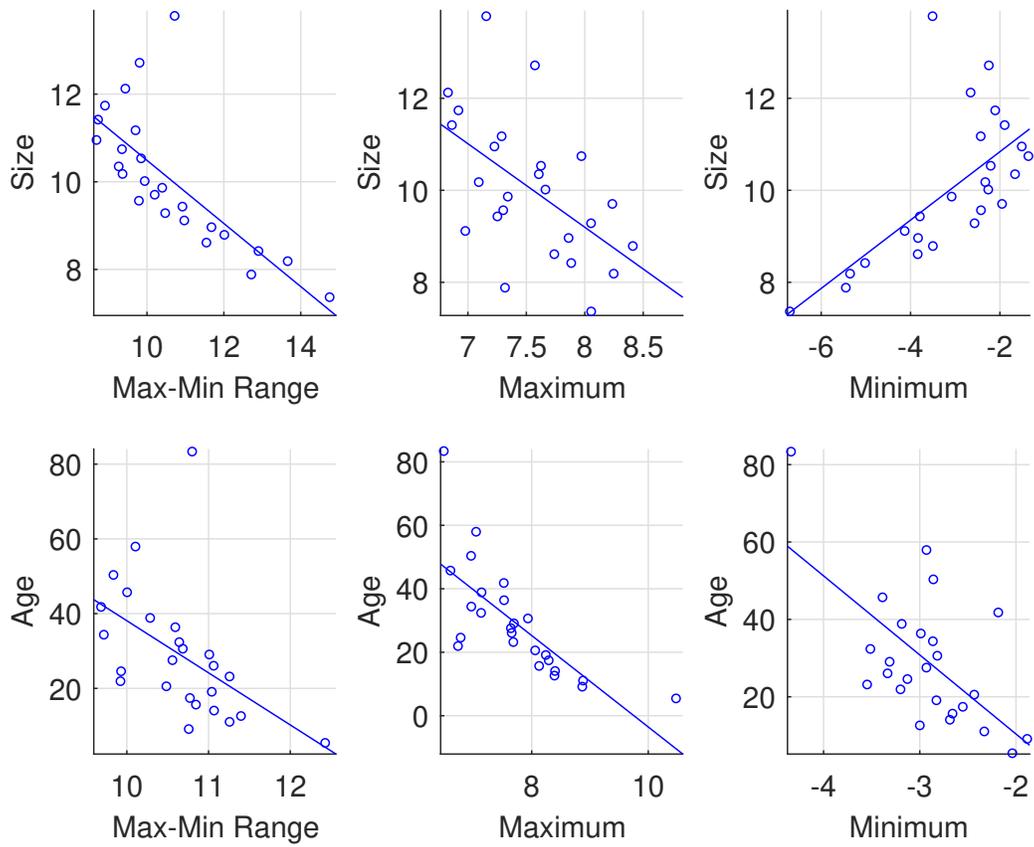


Figure 1: Uncertainty, Age, and Size

Note: Charts report the average sales (or age) and average max-min range for 25 quantiles, computed by pooling observations from 1996 to 2021.

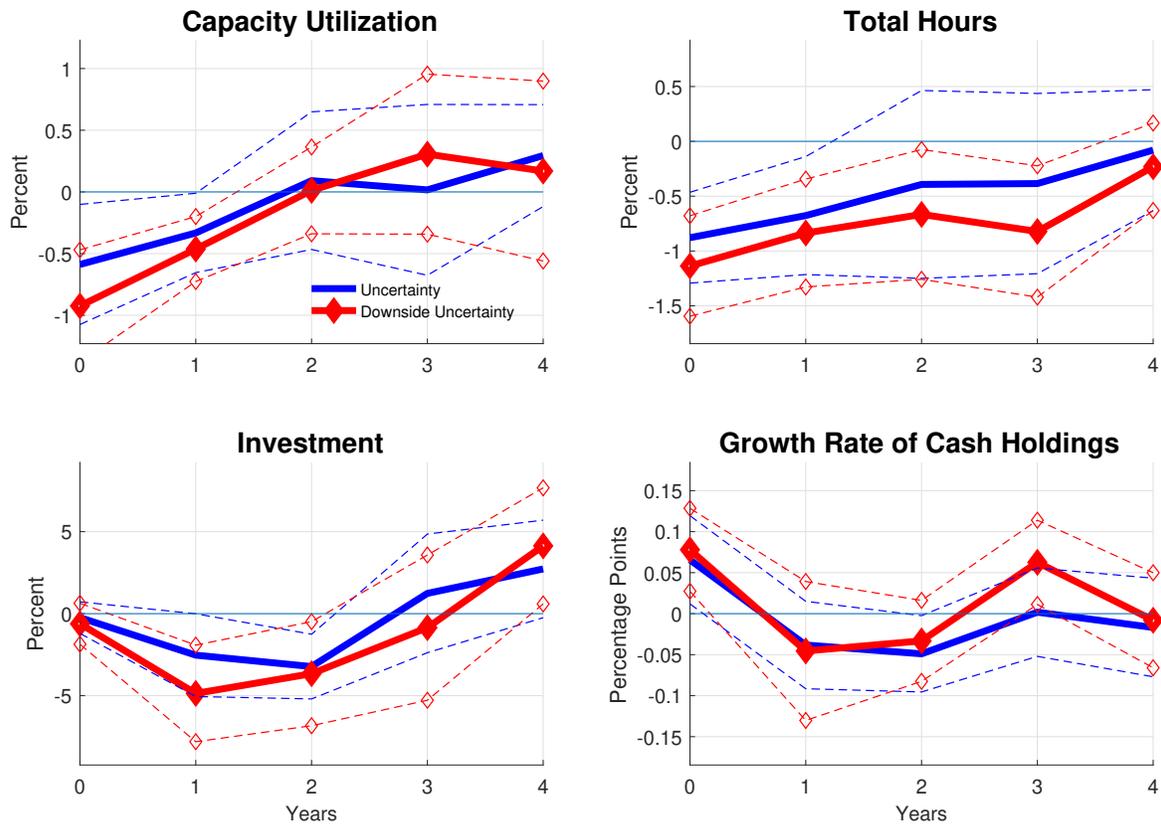


Figure 2: Uncertainty through Downside Uncertainty

Note: In each panel, solid lines report estimated impulse responses following a one standard deviation shock and using coefficients estimates in Tables 4 and 5. Dashed lines report 90 percent confidence intervals.

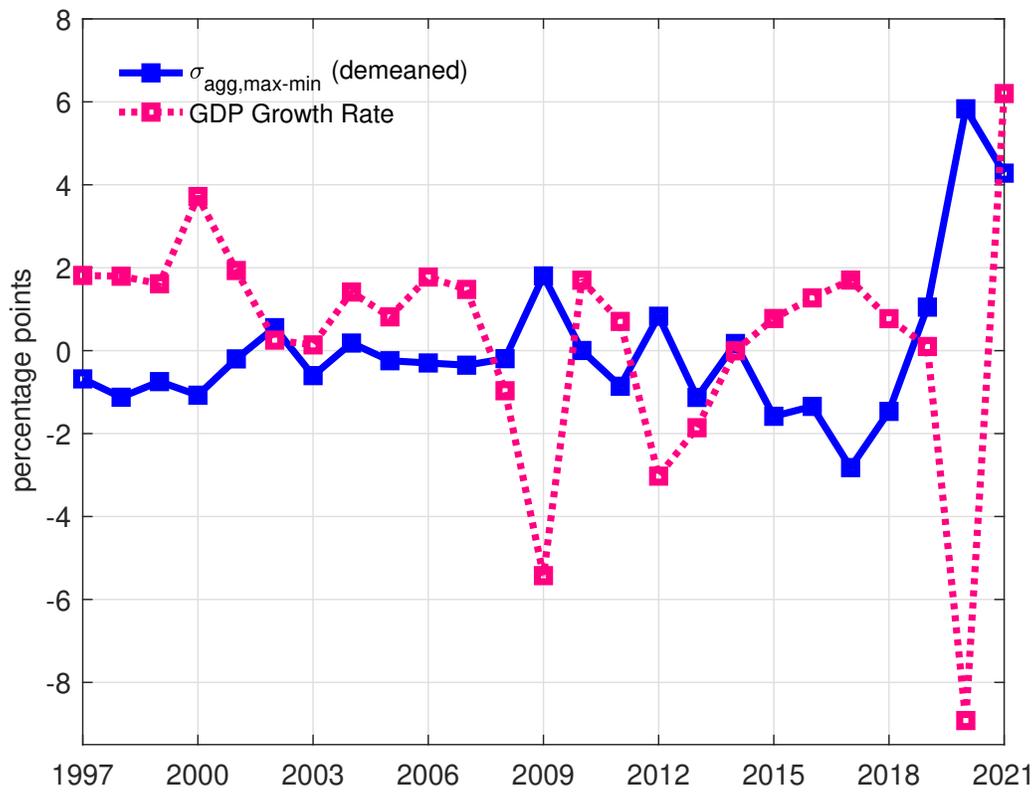


Figure 3: Uncertainty and GDP Growth

Note: The figure reports the demeaned series for aggregate $\sigma_{max-min,agg,t}$, together with the growth rate of real GDP. The sample period runs from 1997 to 2021.

732 ONLINE APPENDIX NOT FOR PUBLICATION

733 **A Data Sources**

734 Our data on expected sales growth (the average, the minimum and the maximum) comes
735 from the Survey of Industrial and Service Firms (INVIND), a large annual business survey
736 conducted by the Bank of Italy on a representative sample of firms. Since 2002, the reference
737 universe in INVIND consists of firms with at least 20 employees operating in industrial sec-
738 tors (manufacturing, energy, and extractive industries) and non-financial private services,
739 with administrative headquarters in Italy. The survey adopts a one-stage stratified sample
740 design. The strata are combinations of the branch of activity (according to an 11-sector clas-
741 sification), size class (in terms of number of employees classified in 7 buckets), and region
742 in which the firm's head office is located. In recent years, each wave has around 4,000 firms
743 (3,000 industrial firms and 1,000 service firms). The data are collected by the Bank of Italy's
744 local branches between February and April every year. The question between the minimum
745 and maximum expected growth rate of sales (min—max gap) covers around 900 firms on
746 average per year, from 1993 to 2007, and 1,677 firms on average per year from 2008 to 2021.
747 The data set has a panel dimension. The firms observed in the previous edition of the sur-
748 vey are always contacted again if they are still part of the target population. In contrast,
749 those no longer wishing to participate are replaced with others in the same branch of activ-
750 ity and size class. To limit the impact of outliers, we winsorize the 1% tails of the max-min
751 range, the minimum, the maximum, the average expected sales, investment, hours, capacity
752 utilization, and cash holdings.

753 **B Heterogeneity in Firm-Level Expectations**

754 Table [A.1](#) describes the properties of firms' expectations conditioning on size, age, and
755 sectors.

Table A.1: Firm-Level Expectations: Descriptive Statistics

	No. of Obs.	Mean	St. Dev.	Skew.	P_{10}	P_{25}	P_{50}	P_{75}	P_{90}
Full Sample									
$s_{avg,f,t}^e$	49674	3.59	11.60	1.00	-7.10	0.00	2.70	7.10	14.50
$s_{min,f,t}^e$	30958	-3.57	10.40	-0.20	-12.00	-10.00	-2.00	1.00	5.00
$s_{max,f,t}^e$	30976	6.91	10.70	1.63	-1.00	1.50	5.00	12.00	15.00
Small and Medium Firms: $20 \leq \text{Labor Force} \leq 50$									
$s_{avg,f,t}^e$	3059	3.53	10.20	1.07	-4.80	0.00	2.40	5.90	14.30
$s_{min,f,t}^e$	5115	-5.97	10.60	-0.42	-14.00	-12.00	-5.00	0.00	4.00
$s_{max,f,t}^e$	5120	6.63	10.40	0.75	-2.00	1.00	5.10	12.00	12.70
Large Firms: Labor Force ≥ 50									
$s_{avg,f,t}^e$	46339	3.60	11.70	0.99	-7.40	0.00	2.80	7.30	14.60
$s_{min,f,t}^e$	25630	-2.14	10.00	-0.01	-12.00	-6.00	-1.00	2.00	7.00
$s_{max,f,t}^e$	25646	7.09	10.80	2.09	-1.00	2.00	5.00	12.00	16.20
Young Firms: Age ≤ 5									
$s_{avg,f,t}^e$	1367	6.27	14.90	1.20	-7.40	0.00	4.00	10.50	22.30
$s_{min,f,t}^e$	873	-3.60	11.60	0.66	-12.00	-12.00	-3.00	1.00	8.00
$s_{max,f,t}^e$	871	9.91	12.00	1.60	0.00	3.00	10.00	12.00	21.00
Old Firms: Age > 5									
$s_{avg,f,t}^e$	48307	3.54	11.50	0.98	-7.00	0.00	2.70	7.10	14.40
$s_{min,f,t}^e$	30085	-3.57	10.30	-0.23	-12.00	-10.00	-2.00	1.00	5.00
$s_{max,f,t}^e$	30105	6.85	10.60	1.62	-1.00	1.50	5.00	12.00	15.00
Manufacturing Sector									
$s_{avg,f,t}^e$	33873	4.28	12.20	0.83	-7.50	0.00	3.50	8.50	16.00
$s_{min,f,t}^e$	21592	-3.08	11.00	-0.26	-12.00	-10.00	-1.20	2.00	7.00
$s_{max,f,t}^e$	21607	7.48	11.20	1.41	-1.00	2.00	5.60	12.00	18.00
Service Sector									
$s_{avg,f,t}^e$	15801	2.55	10.40	1.30	-6.40	-0.10	1.80	5.10	11.30
$s_{min,f,t}^e$	9366	-4.25	9.43	-0.16	-12.00	-12.00	-2.00	0.20	4.00
$s_{max,f,t}^e$	9369	6.14	9.82	2.00	-1.00	1.00	5.00	12.00	12.00

Note: Statistics are computed over the sample period 1996 to 2019, taking into account the sample weight represented by each firm in the entire population of firms. The number of observations refers to the number of firms effectively sampled in the data. Table entries are computed over growth rates (expressed in percent). $s_{avg,f,t}^e$, $s_{min,f,t}^e$, and $s_{max,f,t}^e$ denote the *average*, *minimum*, and *maximum* expected growth rates of sales one year ahead. P_X reports the X^{th} percentile of the distribution.

C Firm-Level Uncertainty

The table below reports descriptive statistics on firm-level uncertainty.

Table A.2: Firm-Level Uncertainty $\sigma_{max-min}$: Descriptive Statistics

No. of Obs.	Mean	St. Dev.	Skew.	P_{10}	P_{25}	P_{50}	P_{75}	P_{90}
<u>Full Sample</u>								
30735	11.00	9.81	1.35	1.00	3.00	8.00	20.00	24.00
<u>Small and Medium Firms: $20 \leq \text{Labor Force} \leq 50$</u>								
5082	13.70	10.60	0.82	1.20	4.00	11.00	24.00	24.00
<u>Large Firms: Labor Force > 50</u>								
25443	9.50	8.99	1.78	1.00	3.00	6.00	13.00	24.00
<u>Young Firms: Age ≤ 5</u>								
866	13.30	10.30	1.05	2.00	5.00	10.00	24.00	24.00
<u>Mature and Old Firms: Age > 5</u>								
29869	11.00	9.79	1.35	1.00	3.00	7.50	20.00	24.00
<u>Manufacturing Sector</u>								
21450	11.00	9.59	1.47	2.00	4.00	8.00	19.00	24.00
<u>Service Sector</u>								
9285	11.00	10.10	1.20	1.00	2.60	7.00	24.00	24.00

Note: Statistics are computed over the sample period 1996 to 2019, weighting firm-specific observations based on their share of the entire population. The number of observations refers to the firms directly observed in the data. $\sigma_{max-min}$ denotes the difference between s_{max}^e and s_{min}^e , the maximum and minimum expected growth rates of sales one year ahead. P_X reports the X^{th} percentile of the distribution.

758 D Downside and Upside Uncertainty: Alternative Proxies

759 The table below reports descriptive statistics on alternative measure of firm-level down-
 760 side, measured as $s_{avg,f,t}^e - s_{min,f,t}^e$, and, and upside uncertainty, measured as $s_{max,f,t}^e - s_{avg,f,t}^e$.
 761 We find that at the firm level $s_{avg,f}^e - s_{min,f}^e$ is acyclical with the correlation with the contem-
 762 poraneous growth rate of real GDP equal to -0.03 and $s_{max,f}^e - s_{avg,f}^e$ slightly countercyclical
 (-0.12).

Table A.3: Alternative Downside and Upside Uncertainty : Descriptive Statistics

	No. of Obs.	Mean	St. Dev.	Skew.	P_{10}	P_{25}	P_{50}	P_{75}	P_{90}
Full Sample									
$s_{avg,f,t}^e - s_{min,f,t}^e$	30735	5.77	6.33	0.50	2.00	4.10	7.40	12.10	
$s_{max,f,t}^e - s_{avg,f,t}^e$	30735	4.24	5.78	0.04	0.70	2.40	5.20	10.10	
Small and Medium Firms: $20 \leq \text{Labor Force} \leq 50$									
$s_{avg,f,t}^e - s_{min,f,t}^e$	5082	4.86	5.99	3.23	0.20	1.00	3.20	6.30	10.10
$s_{max,f,t}^e - s_{avg,f,t}^e$	5082	4.39	6.86	3.20	0.00	0.50	1.70	5.20	12.50
Large Firms: Labor Force > 50									
$s_{avg,f,t}^e - s_{min,f,t}^e$	25443	5.86	6.36	3.46	0.50	2.00	4.30	7.50	12.20
$s_{max,f,t}^e - s_{avg,f,t}^e$	25443	4.23	5.68	3.70	0.00	0.80	2.50	5.20	10.00
Young Firms: Age ≤ 5									
$s_{avg,f,t}^e - s_{min,f,t}^e$	866	7.11	9.01	3.71	0.70	2.69	5.00	7.60	16.00
$s_{max,f,t}^e - s_{avg,f,t}^e$	866	3.59	5.25	7.82	0.00	0.90	2.50	5.00	8.00
Mature and Old Firms: Age > 5									
$s_{avg,f,t}^e - s_{min,f,t}^e$	29869	5.75	6.27	3.39	0.50	2.00	4.10	7.40	12.10
$s_{max,f,t}^e - s_{avg,f,t}^e$	29869	4.26	5.78	3.60	0.00	0.70	2.40	5.20	10.20
Manufacturing Sector									
$s_{avg,f,t}^e - s_{min,f,t}^e$	21450	6.22	6.64	3.40	0.50	2.20	4.80	8.00	13.00
$s_{max,f,t}^e - s_{avg,f,t}^e$	21450	4.45	5.81	3.42	0.00	0.80	2.70	5.60	10.60
Service Sector									
$s_{avg,f,t}^e - s_{min,f,t}^e$	9285	4.85	5.54	3.46	0.40	1.50	3.20	6.00	10.60
$s_{max,f,t}^e - s_{avg,f,t}^e$	9285	3.81	5.68	4.20	0.00	0.60	2.00	4.80	9.30

Note: Statistics are computed over the sample period 1996 to 2019, weighting firm-specific observations based on their share of the entire population. The number of observations refers to the firms directly observed in the data. $s_{avg,f,t}^e$, $s_{max,f,t}^e$ and $s_{min,f,t}^e$ denote the average, maximum, and minimum expected growth rates of sales one year ahead. P_X reports the X^{th} percentile of the distribution.

764 Below we show the estimated effects of firm-level uncertainty when downside and up-
765 side uncertainty are proxied by $s_{avg,f,t}^e - s_{min,f,t}^e$ and $s_{max,f,t}^e - s_{avg,f,t}^e$ respectively. As dis-
766 cussed in Section 5, downside uncertainty drives the economic effects of total uncertainty.
767 Upside uncertainty does not result in appreciable economic effects.

Table A.4: Alternative Proxies of Downside and Upside Uncertainty

Panel A - Increase in Alternative Downside Uncertainty 1 p.p.					
Horizon=h	0	1	2	3	4
<i>Capacity Util. (t+h)</i>	-0.169*** (0.01)	-0.054 (0.56)	0.043 (0.84)	0.123** (0.02)	0.116 (0.15)
<i>Total Hours (t+h)</i>	-0.157*** (0.00)	-0.105* (0.10)	-0.130* (0.11)	-0.171** (0.03)	-0.030 (0.32)
<i>Real Investment (t+h)</i>	-0.128 (0.71)	-0.120 (0.98)	-0.622* (0.09)	-0.987 (0.27)	1.080* (0.10)
<i>Growth Rate of Cash Holdings (t+h)</i>	0.019* (0.10)	0.007 (0.81)	0.005 (0.32)	-0.010* (0.05)	0.001 (0.80)
Panel B - Increase in Alternative Upside Uncertainty 1 p.p.					
Horizon=h	0	1	2	3	4
<i>Capacity Util. (t+h)</i>	-0.016 (0.79)	-0.004 (0.97)	0.048 (0.69)	-0.097 (0.27)	0.047 (0.20)
<i>Total Hours (t+h)</i>	-0.096 (0.13)	-0.093 (0.15)	-0.046 (0.53)	0.077 (0.51)	0.051 (0.44)
<i>Real Investment (t+h)</i>	0.399 (0.48)	-0.601 (0.40)	-0.367 (0.32)	0.571 (0.29)	0.596 (0.26)
<i>Growth Rate of Cash Holdings (t+h)</i>	-0.008 (0.33)	-0.014 (0.06)	-0.001 (0.91)	-0.011 (0.27)	-0.007 (0.48)

Note: The table reports ordinary least squares estimates of the coefficient $\beta_{avg-min,h}$ in Panel A and $\beta_{max-avg,h}$ in Panel B in Equation 2 with downside and upside uncertainty now proxied by $s_{avg,f,t}^e - s_{min,f,t}^e$ and $s_{max,f,t}^e - s_{avg,f,t}^e$ respectively. The sample period runs from 1996 to 2019. P-values are shown in parentheses. Stars denote the significance level of the coefficient they refer to: * p-value<0.10, ** p-value<0.05, and *** p-value<0.01. Standard errors clustered by firm and year. Entries, except for cash holdings in percentage points, are expressed in percent. Panel A reports the response of each variable to a 1 percentage point increase in $s_{avg,f,t}^e - s_{min,f,t}^e$ or equivalently an increase in downside uncertainty. Panel B reports the response of each variable to a 1 percentage point increase in $s_{max,f,t}^e - s_{avg,f,t}^e$ or, equivalently, an increase in upside uncertainty.